

ENERGY-EFFICIENT VLSI IMPLEMENTATION OF MULTIPLIERS WITH DOUBLE LSB OPERANDS

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Abstract: Redundant Binary Partial Product Generator technique are used to reduce by one row the maximum height of the partial product array generated by a radix16 Modified Booth Encoded multiplier, without any raise in the delay of the partial product creation Block. In this paper, we describe an optimization for binary radix-4 modified Booth recoded multipliers to reduce the maximum height of the partial product columns to $\lceil n/4 \rceil$ for $n = 64$ -bit unsigned operands. This is in contrast to the conventional maximum height of $\lceil (n + 1)/4 \rceil$. Therefore, a reduction of one unit in the maximum height is achieved. This Arithmetic multipliers increase the performance of ALU and Processors. We evaluate the proposed approach by comparison with Normal Booth Multiplier. Logic synthesis showed its efficiency in terms of area, delay and power. Simulation results show that the proposed Multiplier based designs significantly improve the area, delay and power consumption when the word length of each operand in the multiplier is 64 & n-bits. The proposed architecture of this paper analysis the delay and area using Xilinx 14.2.

Keywords: Modified Booth Encoding, Radix-16, Pipeline, Multiplier, Enhanced, Carry Select Adder, Binary Excess Converter.

1. Introduction

Multiplier is one of the basic hardware block used for many digital and high performance systems such as FIR filters, digital signal processors and microprocessors etc. Many high speed low power multiplication algorithms and architectures have been proposed. Advances in technology have permitted many researchers to design multipliers which offer both high-speed and regularity of layout, thereby making them suitable for VLSI implementation. Digital signal processing requires efficient multiplication operations with the highest possible speed without compromising the power budget. In general, basic multiplication algorithm can be divided into

three following steps. 1) partial product (pp) generation, 2) partial product reduction and 3) final carry propagated addition [1-2]. In the first step, a set of partial product rows is generated where each one is the result of the product of one bit of the multiplier by multiplicand. For example, if we consider the multiplication $X \times Y$ with both X and Y on n bits and of the form $x_{n-1} \dots x_0$ and $y_{n-1} \dots y_0$, then the i th row is, in general, a proper left shifting of $y_i \times X$, i.e., either a string of all zeros when $y_i = 0$, or the multiplicand X itself when $y_i = 1$. In this case, the number of PP rows generated during the first phase is clearly n [1-4]. Recoding of binary numbers was first hinted at by Booth [5] four decades ago.

MacSorley[6] proposed a modification of Booth's algorithm a decade after. Modified booth encoding (MBE) [6] is a technique that has been introduced to reduce the no of pp rows with a maximum height of $\lceil n/2 \rceil + 1$ rows. More specifically, Two's complement multiplier [7] using radix-4 MBE generates a pp array with a maximum height of $\lceil n/2 \rceil$ rows without any increase of delay, each row of the pp array follows the one of the following possible values: all zeros, +X, +2X [8]. This pp reduction may increase the speed of the multiplier. During pp reduction phase, all pp rows are reduced by using compression tree [9-10]. Since the intermediate addition values is not important, the outcome of this phase is a result represented in redundant carry save form, i.e., as two rows, which allows for much faster implementations. The final (carry-propagated) addition has the task of adding these two rows and of presenting the final result in a non-redundant form, i.e., as a single row. In this work, we introduce an idea to reduce the pp array with a maximum height of $\lceil n/3 \rceil$ rows by using radix-8 booth recoding process. A similar study aimed at the reduction of the maximum height to $\lceil n/3 \rceil$ but using a different approach has recently presented interesting results in [11]. Thus, in the following, we will evaluate and compare the proposed approach with the technique in [7].

2. LITERATURE SURVEY

The conventional modified Booth encoding (MBE) generates an irregular partial product array because of the extra partial product bit at the least significant bit position of each partial product row. In this brief, a simple approach is proposed to generate a regular

partial product array with fewer partial product rows and negligible overhead, thereby lowering the complexity of partial product reduction and reducing the area, delay, and power of MBE multipliers. The proposed approach can also be utilized to regularize the partial product array of post truncated MBE multipliers. Implementation results demonstrate that the proposed MBE multipliers with a regular partial product array really achieve significant improvement in area, delay, and power consumption when compared with conventional MBE multipliers. Complex arithmetic operations are widely used in Digital Signal Processing (DSP) applications. In this work, we focus on optimizing the design of the fused Add-Multiply (FAM) operator for increasing performance. We investigate techniques to implement the direct recoding of the sum of two numbers in its Modified Booth (MB) form. We introduce a structured and efficient recoding technique and explore three different schemes by incorporating them in FAM designs. Comparing them with the FAM designs which use existing recoding schemes, the proposed technique yields considerable reductions in terms of critical delay, hardware complexity and power consumption of the FAM unit.

3. EXISTING METHOD

The Booth algorithm has been used to improve the sign correction issues of signed number multiplication; however, the original Booth algorithm does not reduce the number of PPs. A Modified Booth Encoding (MBE) method (also known as the radix-4 Booth algorithm) has been further proposed. It reduces the number of PP rows by half. The complexity of the parallel multiplier is

reduced significantly by applying MBE. The power consumption and the delay of the entire multiplier are also reduced. Let $A = a_{N-1}a_{N-2} \dots a_2a_1a_0$ be the multiplicand and $B = b_{N-1}b_{N-2} \dots b_2b_1b_0$ be the multiplier. The multiplier bits are encoded; so they are grouped in sets of three adjacent bits. The two side bits overlap with neighboring groups, except the first multiplier bit group. As per the encoded results from A, the Booth decoders select $-2A$, $-A$, 0 , A , or $2A$ to generate the PP rows. $2A$ is obtained by a simple 1-bit left shift of the multiplicand. The negation operation is achieved by inverting each bit of A and adding 1 at its least significant bit (LSB) position. This is referred to as the correction term in this work. Therefore, the PP of each line can be easily generated by either shifting or inverting the multiplicand bits. The circuit diagram of the MBE scheme is shown in Fig. 2. Table 1 shows the K-Map of a conventional MBE. Therefore, the output of the Booth encoder pp_{ij} is given as follows:

$$pp_{ij} = (b_{2i} \oplus b_{2i-1})(b_{2i+1} \oplus a_j) + (b_{2i} \oplus b_{2i-1})(b_{2i+1} \oplus b_{2i})(b_{2i+1} \oplus a_{j-1}) \quad (1)$$

The correction term for the negation operation is as follows:

$$E_i = b_{2i+1}b_{2i} + b_{2i+1}b_{2i-1} \quad (2)$$

As per Eq. (2), the correction term (i.e., E_i) of the negation operation is almost equal to the MSB of the multiplier except when $b_{2i+1}b_{2i}b_{2i-1} = 111$. E_i can be further simplified by reconsidering this entry in the MBE truth table. In [36], it is observed that all the entries in the 6th column of Table 1 can be changed to 1 to achieve a simplified E_0 along with a slight increase in complexity of a pp_{0ij} as follows:

$$pp_{0ij} = (b_{2i} \oplus b_{2i-1})(b_{2i+1} \oplus a_j) + (b_{2i} \oplus b_{2i-1})(b_{2i+1} \oplus b_{2i})(b_{2i+1} \oplus a_{j-1}) + b_{2i+1}b_{2i}b_{2i-1} \quad (3)$$

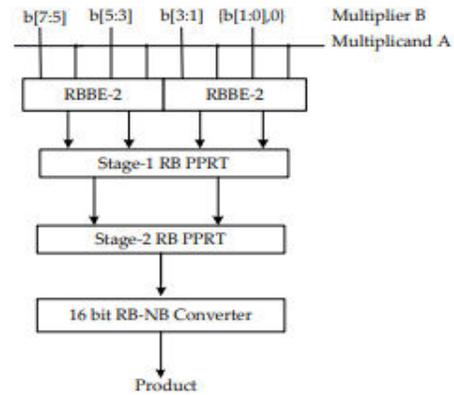


Fig. 1. Overall structure of an 8-bit RB multiplier

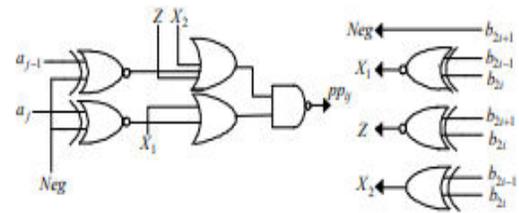


Fig. 2. MBE scheme: encoder and decoder

4. PROPOSED METHOD

The K-map of the radix-4 approximate modified Booth encoder (R4AMBE6), i.e., app_{ij6-1} , with 6 errors in the Kmap is shown in Table 1, where 0 denotes an entry in which a '1' is replaced by a '0' and 1 denotes a '0' entry that has been replaced by a '1'. Only 6 entries are modified to simplify the Booth encoding. This approximate design relies on the property that the truth table is as symmetrical as possible for a design with the least complexity. Therefore, three modifications change a '1' to a '0' and three modifications change a '0' to a '1' in the K-map. The output of R4AMBE6 is given as follows:

$$app_{ij6-1} = (b_{2i} + b_{2i-1})(b_{2i+1} \oplus a_i) \quad (17)$$

$$E_i = (b_{2i+1}b_{2i}) + (b_{2i+1}b_{2i-1})$$

Compared with the exact MBE, R4AMBE6 can significantly reduce both the complexity and the critical path delay of Booth encoding. The error rate, denoted by P_{be} , is given by: $P_{be} = 6/32 = 18.75\%$ (19) The gate level structure of R4AMBE6 is shown in Fig. 5. The conventional design of MBE (Fig. 2) consists of four XNOR-2 gates, one XOR-2 gate, one OR-3 gate, one OR2 gate and one NAND-2 gate. The R4AMBE6 design only requires one XOR-2 gate, one AND-2 gate and one OR-2 gate

The approximate Radix-4 with the new modified Booth Encoding (R4ANMBE6), i.e., app_{0ij6-1} , with 6 errors in the K-map is shown in Table 1. In this approximate design, there are more entries changed from '0' to '1' than those changed from '1' to '0'. Therefore, the approximate results produced by R4ANMB6 will be usually larger than its exact counterpart.

TABLE 1: K-Map of R4AMBE6

$a_j a_{j-1}$ \ $b_{2i+1} b_{2i} b_{2i-1}$	000	001	011	010	110	111	101	100
00	0	0	0	0	1	1	1	0
01	0	0	0	0	1	1	1	0
11	0	1	1	1	0	0	0	0
10	0	1	1	1	0	0	0	0

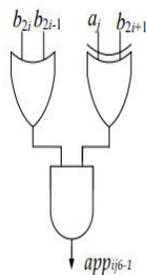


Fig. 3. The gate-level circuit of the proposed R4AMBE6

From Table 1, the approximate pp_{0ij} is derived as follows:

$$app_{0ij6-1} = b_{2i+1} \oplus a_j + b_{2i}b_{2i-1} \quad (20) \quad E$$

$$0 \leq i < n$$

This design further reduces the complexity of the correction term (i.e., E_i). Its error rate is the same as R4AMBE6: The gate level circuit of R4ANMBE6 is shown in Fig. 4. The R4AMBE6 design only requires one XOR-2 gate, one AND-2 gate and one OR-2 gate, which has the same complexity as R4AMBE6

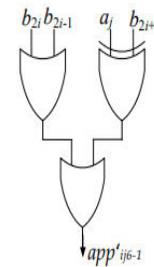


Fig. 4. The gate-level circuit of the proposed R4AMBE6

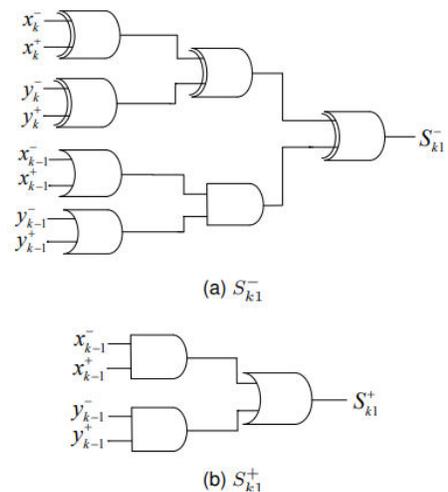


Fig. 5. The gate level circuit of ARBC-1

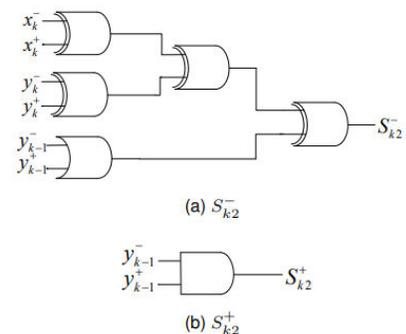


Fig. 6. The gate level circuit of ARBC-2
 Efficient designs must ensure that the error between the approximate RB compressor and its exact counterpart remains as small as possible. The final results of compression are the same when $(x - k, x + k)$ is equal to either (1, 0) or (0, 1). So, when the result of the approximate RB compressor is $(x - k, x + k) = (1, 0)$ rather than the exact compression result $(x - k, x + k) = (0, 1)$, the result is still correct. Therefore, the following four types of compression results are equivalent: $(0, 0) = (0, 0)$, $(0, 1) = (1, 0)$, $(1, 0) = (0, 1)$ and $(1, 1) = (1, 1)$.

The Proposed accurate RB-NB Converter

As the approximate Booth encoders and approximate RB compressors generate results that are generally larger than the exact results, the biased approximate results can be compensated using ARNC with smaller values. The principle of compensation is to use an approximate adder that produces results that are smaller than its exact results. Therefore, the complexity of the RB-NB converter can be reduced, while the overall accuracy of the approximate RB multipliers is also increased. The truth table of a possible approximate RB-NB converter is given by Table 6, a simple NOR gate is used in the approximate RB-NB digit converter as follows: $S_0 k = S - k + S + k$ (29) In this section, the approximate RB multipliers are designed as follows. The proposed approximate Booth encoders, i.e., R4AMBE6 and R4ANMBE6, are used to generate approximate PPs. Approximate RB compressors, i.e., ARBC-1 and ARBC-2, are used for RB PP reduction, which can reduce the delay for compression and significantly improve speed performance when the

operand size is a power of 2. The approximate RB-NB converter neither (made of NOR gates) is used to convert the RB digit to the NB digit. An approximation factor p ($p=1, 2, \dots, 2N$) that has been proposed is used. This is defined as the number of least significant PP columns that are generated by the approximate Booth encoders.

TABLE 2: The Truth Table of RB-NB Conversion

RB Digit (S_k^+, S_k^-)	Carry-in(C_k)	ENB (S_k)	ANB1 (S'_{k1})	ANB2 (S'_{k2})	ANB3 (S'_{k3})
(0,0)	0	1	1	1	1
(0,0)	1	0	1	1	1
(0,1)	0	0	0	1	0
(0,1)	1	1	0	1	0
(1,0)	0	0	0	1	0
(1,0)	1	1	0	1	0
(1,1)	0	1	0	0	1
(1,1)	1	0	0	0	1

As p column PPs are already approximate, the approximate PPs can be accumulated with an approximate RB 4:2 compressor to further improve speed and reduce power consumption. For the same reason, the p least significant RB digits are also converted by the approximate RB-NB converter to calculate the final product. Four approximate RB multipliers are proposed. They use the exact regular PP array when $p \leq (N - 4)$ (as detailed in [36]), and the approximate regular PP array when $p > (N - 4)$ where the bit pairs (E2, 0) and (E3, 1) of Fig. 4 can be ignored in the approximate design of the RB Booth multipliers; however they all use the proposed approximate RB-NB converter. For the $2N-p$ most significant PP columns, the exact design is used for the final results. The four RB multipliers are different in the p PP columns as follows:

- 1) The first approximate RB multiplier (R4ARBM1) uses R4AMBE6 to generate the p least significant PP columns and ARBC-1 to perform the approximate PP accumulation.
- 2) The second approximate RB multiplier (R4ARBM2) uses R4AMBE6 to generate the p least significant PP columns and ARBC-2 for the corresponding approximate PP accumulation.
- 3) The third approximate RB multiplier (R4ARBM3) uses R4ANMBE6 to generate the p least significant PP columns and ARBC-1 to perform the approximate PP accumulation.
- 4) The fourth approximate RB multiplier (R4ARBM4) uses R4ANMBE6 to generate the p least significant PP columns and ARBC-2 to perform the approximate PP accumulation. As the error can be controlled by the approximation factor p , a reasonable accuracy can be achieved for different applications.

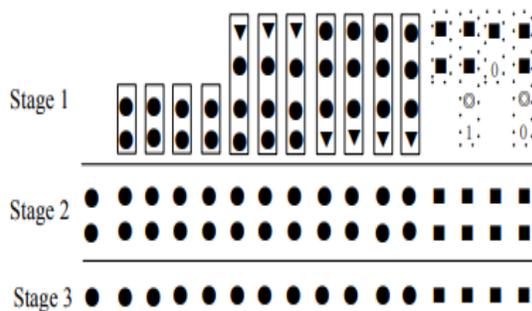


Fig. 9. The dot diagram of the proposed 8-bit approximate RB multiplier

Fig. 9 shows an approximate 8-bit RB multiplier with $p=4$ using an approximate Booth encoder, an approximate RB compressor, an approximate RB-NB converter, and an exact regular PP. A box with a solid line denotes the use of an exact

RB compressor, and a box with a dotted line denotes an approximate RB 4:2 compressor. The exact PP is represented by \bullet , the modified PP after logic simplification is represented by \blacktriangledown , while the approximate PP term is represented by E_i .

5. SIMLUATION RESULTS

The developed project is simulated and verified their functionality. Once the functional verification is done, the RTL model is taken to the synthesis process using the Xilinx ISE tool. In synthesis process, the RTL model will be converted to the gate level netlist mapped to a specific technology library. Here in this Spartan 3E family, many different devices were available in the Xilinx ISE tool. In order to synthesis this design the device named as “XC3S500E” has been chosen and the package as “FG320” with the device speed such as “-5”. This design is synthesized and its results were analyzed as follows:

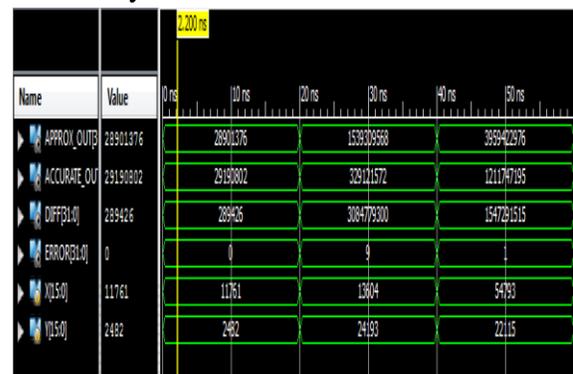


Fig 7: SIMULATION RESULT

Device Utilization Summary (estimated values)			
Logic Utilization	Used	Available	Utilization
Number of Slice LUTs	157	17600	0%
Number of fully used LUT-FF pairs	0	157	0%
Number of bonded IOBs	64	100	64%
Number of DSP48E1s	2	80	2%

Fig 8: PROPOSED DESIGN SUMMARY

Cell:in->out	fanout	Gate Delay	Net Delay	Logical Name (Net Name)
IBUF:I->O	10	0.000	0.592	Y_5_IBUF (Y_5_IBUF)
LUT6:I0->O	1	0.043	0.343	L2/Mmux_out23 (L2/Mmux_out22)
LUT3:I1->O	1	0.043	0.428	L2/Mmux_out25_SWO (N10)
LUT6:I3->O	27	0.043	0.395	L2/Mmux_out25 (out4y<1>)
LUT6:I5->O	7	0.043	0.578	T2/GND_3_o_GND_3_o_sub_15_OUT<1>11 (T2/GND_3_o_GND_3_o)
LUT6:I0->O	1	0.043	0.000	T2/Mmux_out2<2>_51 (T2/Mmux_out1<3>_51)
MUXF7:I1->O	1	0.172	0.000	T2/Mmux_out1<3>_4_f7 (T2/Mmux_out1<3>_4_f7)
MUXF8:I0->O	2	0.123	0.284	T2/Mmux_out1<3>_2_f8 (YAT<6>)
DSP48E1:A3->P1	2	2.823	0.433	A1/Maddsub_mult (out1<1>)
LUT3:I0->O	8	0.043	0.582	Sh11 (Sh1)
LUT6:I0->O	1	0.043	0.279	Sh811 (Sh81)
OBUF:I->O		0.000		out_17_OBUF (out<17>)
Total		7.334ns	(3.419ns logic, 3.915ns route)	(46.6% logic, 53.4% route)

Fig 9: PROPOSED TIMING REPORT

Fig 10: POWER SUMMARY

Table 3: COMPARISION TABLE

	EXISTIN G	PROPOSE D
LUTS	195	157
TIME DELAY	25.418ns	7.334ns
POWER CONSUMPTIO N	0.114w	0.065w

5. CONCLUSION: The multiplier using the proposed algorithm achieves better power-delay products than those achieved by conventional Booth multipliers. Here, we have presented a method to reduce by one the maximum height of the partial product

array for 64-bit, 128-bit radix-4 Booth recoded magnitude multipliers. This reduction may allow more flexibility in the design of the reduction tree of the pipelined multiplier and achieved with no extra delay for $n \geq 32$ for a cell-based design.. We believe that the proposed Booth algorithm can be broadly utilized in general processors as well as digital signal processors, mobile application processors, and various arithmetic units that use Booth encoding.

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